

# C11 - 9.2 - Linear/Quadratic Inequalities In One Variable Notes

## Solve

$$x - 2 \leq 0$$

$$x - 2 \leq 0$$

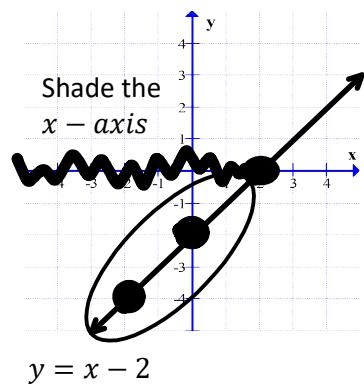
$$+2 \quad +2$$

Solve

$$x \leq 2$$

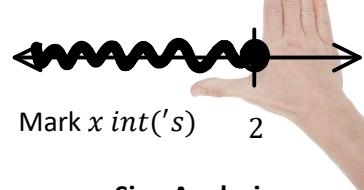
Graphing

$y$  values  $\leq 0$   
The Thing  $\leq 0$



What are the  $x$  values when  $y \leq 0$ . Circle them!

### Number Line



### Sign Analysis

Pick a value

$$x \leq 2 \quad x \geq 2$$

$$x = 0 \text{ Substitute } x = 4$$

$$\begin{array}{ll} x - 2 \leq 0 & x - 2 \leq 0 \\ 0 - 2 \leq 0 & 4 - 2 \leq 0 \\ -2 \leq 0 & 2 \leq 0 \end{array}$$

Correct:  
Shade that section

Incorrect:  
Shade Not that section

$$x \leq 2$$

$$-x^2 + 5x - 4 < 0$$

$$-x^2 + 5x - 4 < 0$$

$$-(x^2 - 5x + 4) < 0$$

$$\frac{(x^2 - 5x + 4)}{-1} > \frac{0}{-1}$$

$$x^2 - 5x + 4 > 0$$

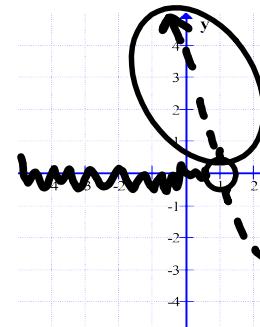
$$(x - 4)(x - 1) > 0$$

$x$  - intercept's

$$x - 4 = 0 \quad x - 1 = 0$$

$$x = 4 \quad x = 1$$

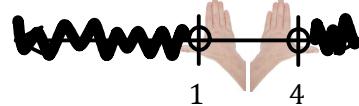
$y$  values  $> 0$   
The Thing  $> 0$



$$y = (x - 4)(x - 1)$$

What are the  $x$  values when  $y > 0$ . Circle them!

### Number Line



### Sign Analysis

Pick a value

$$x < 1 \quad 1 < x < 4 \quad x > 4$$

$$x = 0 \quad x = 2 \quad x = 5$$

Substitute

$$(x - 4)(x - 1) > 0 \quad (1)(4) > 0 \quad 4 > 0$$

$$(0 - 4)(0 - 1) > 0 \quad (-4)(-1) > 0 \quad 4 > 0$$

$$(-2)(1) > 0 \quad -2 > 0$$

$$x < 1 \quad x > 4$$

$$x^2 - 4 \leq 0$$

$$x^2 - 4 \leq 0$$

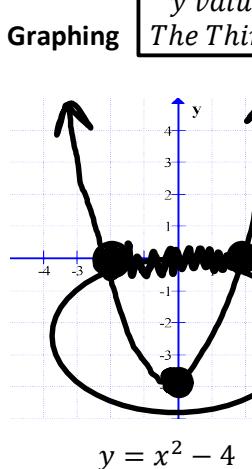
$$(x + 2)(x - 2) \leq 0$$

$$x + 2 = 0 \quad x - 2 = 0$$

$$x = -2 \quad x = 2$$

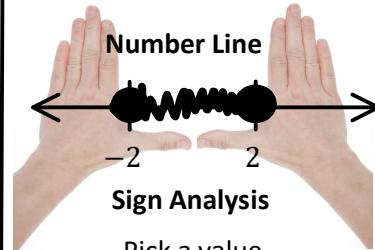
$x$  - intercept's

$y$  values  $\leq 0$   
The Thing  $\leq 0$



$$y = x^2 - 4$$

What are the  $x$  values when  $y \geq 0$ . Circle them!



### Number Line

Sign Analysis

Pick a value

$$x \leq -2 \quad -2 \leq x \leq 2 \quad x \geq 2$$

$$x = -3 \quad x = 0 \quad x = 3$$

$$x^2 - 4 \leq 0 \quad (-3)^2 - 4 \leq 0 \quad (3)^2 - 4 \leq 0$$

$$5 \leq 0 \quad 5 \leq 0 \quad 5 \leq 0$$

$$x^2 - 4 \leq 0 \quad (0)^2 - 4 \leq 0 \quad 5 \leq 0$$

$$5 \leq 0 \quad 5 \leq 0 \quad 5 \leq 0$$

$$-2 \leq x \leq 2$$

The answer is only the Domain. The number line and graph is only to help. There is no  $y$  involved.