

C11 - 7.7 - Linear Reciprocals Notes

$$y = x + 4$$

Line

$$y = \frac{1}{x + 4}$$

Reciprocal line

Pick a y value, What's one divided by that y value. Put a point on the graph. X value is same as it was.

Solve algebraically: set denominator = 0, 1, -1.

Vertical asymptote (VA):
Denominator = 0

$$\begin{aligned} x + 4 &= 0 \\ x &= -4 \end{aligned}$$

$$\text{VA: } x = -4$$

$$D: x \neq -4$$

Invariant points (IP):
Denominator = 1

$$\begin{aligned} x + 4 &= 1 \\ x &= -3 \end{aligned}$$

$$(-3, 1)$$

Invariant points (IP):
Denominator = -1

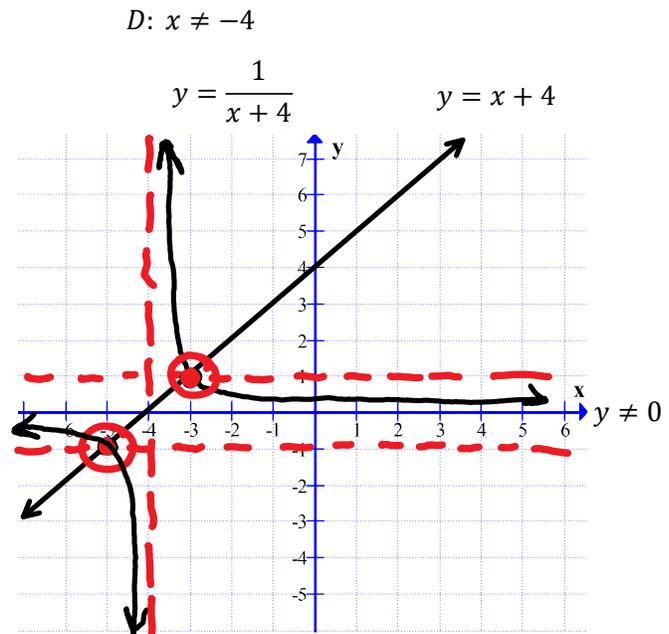
$$\begin{aligned} x + 4 &= -1 \\ x &= -5 \end{aligned}$$

$$(-5, -1)$$

1. Graph original
2. Graph VA: Dotted line
3. Graph IP's
4. Graph reciprocal

x	y
-5	-1
-4	0
-3	1

x	$\frac{1}{x + 4}$
-100	-.01
-5	-1
-4.1	-10
-4.01	-100
-4	UND
-3.99	100
-3.9	10
-3	1
100	.01



Notice: The invariant points are the intersection of the original and the lines $y = 1, y = -1$

Notice: The vertical asymptote(s) of the reciprocal is the X intercept of the original

