

M9 - 3.0 - Exponents Review

7² Exponent Base **Remember:**
-Never multiply base by the exponent
-Must have same base to use laws.

Rule: $2^3 \times 2^2 = 2^{3+2} = 2^5 = 32$ ✓ **Theory:** $2^3 \times 2^2 = (2 \times 2 \times 2) \times (2 \times 2) = 2^5$ *Add exponents*

$\frac{3^5}{3^2} = 3^{5-2} = 3^3 = 27$ ✓ $\frac{3^5}{3^2} = \frac{3 \times 3 \times 3 \times 3 \times 3}{3 \times 3} = 3^3$ *Subtract exponents*

$(2^2)^3 = 2^{2 \times 3} = 2^6 = 64$ ✓ $(2^2)^3 = (2 \times 2) \times (2 \times 2) \times (2 \times 2) = 2^6$ *Multiply exponents*
Distribute exponents

$(2^1 x^1)^3 = 2^3 x^3 = 8x^3$ ✓ $(2x)^3 = (2x) \times (2x) \times (2x) = 8x^3$ $a^b \times c^b = (a \times c)^b$
 $\left(\frac{3}{5}\right)^2 = \frac{3^2}{5^2} = \frac{9}{25}$ ✓ $\left(\frac{3}{5}\right)^2 = \frac{3}{5} \times \frac{3}{5} = \frac{3^2}{5^2} = \frac{9}{25}$ $\frac{a^b}{c^b} = \left(\frac{a}{c}\right)^b$

Step 1 ← Over

$2^{-3} = \frac{1}{2^3} = \frac{1}{8}$ ✓ *Bring to the bottom*
Make exponent positive $\left(\frac{a}{b}\right)^{-c} = \left(\frac{b}{a}\right)^c$

$\frac{1}{3^{-2}} = \frac{3^2}{1} = 9$ ✓ *Bring to the top*
Make exponent positive $\frac{4^{-2}}{2^{-3}} = \frac{2^3}{4^2} = \frac{8}{16} = \frac{1}{2}$

$\frac{3^{-2} + 1}{5} = \frac{\frac{1}{3^2} + 1}{5}$ ✓ $\frac{3^{-2} + 1}{5} \neq \frac{1}{3^2 5}$

$-2^2 = -2 \times 2 = -4$ ✓ $-2^2 = (-2^2)$ *WITHOUT brackets stay NEGATIVE* **Negative Numbers**

$(-2)^2 = (-2) \times (-2) = 4$ ✓ *WITH brackets to EVEN exponents become POSITIVE*

$(-4)^3 = (-4) \times (-4) \times (-4) = -64$ ✓ *WITH brackets to ODD exponents stay NEGATIVE*

$5^0 = 1$ ✓ *Anything (nonzero) to the 0 is 1.* $1^{12} = 1$ ✓ *1 to the anything is 1.*

$8^1 = 8$ ✓ *Anything to the 1 is itself.* $0^5 = 0$ ✓ *0 to the (positive) anything* is 0.*

Change of Base

Theory

$3^3 = 27$ $\div 3$
 $3^2 = 9$ $\div 3$
 $3^1 = 3$ $\div 3$
 $3^0 = 1$ $\div 3$
 $3^{-1} = \frac{1}{3^1} = \frac{1}{3}$ $\div 3$
 $3^{-2} = \frac{1}{3^2} = \frac{1}{9}$ $\div 3$

$3 \times 3 = 3^2$ ✓
 $3 \times 3^2 = 3^3$ ✓

$\frac{3^3}{3^2} = \frac{3 \times 3 \times 3}{3 \times 3} = 3$ ✓ $\frac{3^3}{3^2} = 3$
 $\frac{3^2}{3^1} = \frac{3 \times 3}{3} = 3$ ✓ $\frac{3^2}{3^1} = 3$
 $\frac{3^3}{3^3} = \frac{3 \times 3 \times 3}{3 \times 3 \times 3} = 3^0 = 1$ ✓ $\frac{3^3}{3^3} = 3^0 = 1$
 $\frac{3^1}{3^2} = \frac{3}{3 \times 3} = \frac{1}{3}$ ✓ $\frac{3^1}{3^2} = \frac{1}{3}$
 $\frac{3^0}{3^3} = \frac{1}{3 \times 3 \times 3} = \frac{1}{27}$ ✓ $\frac{3^0}{3^3} = \frac{1}{3^3} = \frac{1}{27}$