

M8 - 3.2 - Solving Square Roots Prime Factorization Notes

Perfect Square: A number that is the product of the same two factors. $9 = 3 \times 3 = 3^2$

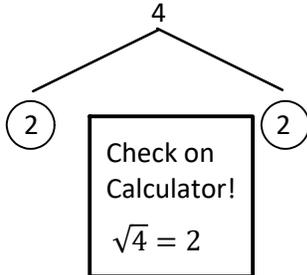
3



3

$\sqrt{9} = 3$ $3^2 = 3 \times 3 = 9$

$\sqrt{4} = ?$



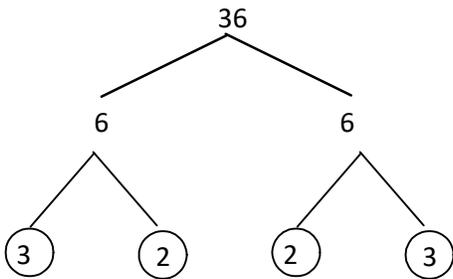
4 is a perfect square because it is a product of the same two factors: 2 and 2.

$$\begin{aligned} \sqrt{4} &= \sqrt{2 \times 2} \\ \sqrt{4} &= \sqrt{2 \times 2} \\ &= 2 \end{aligned}$$

Two identical numbers under a square root: one comes out. Nothing is left.

OR Think about two identical numbers that multiply together to make that number

$\sqrt{36} = ?$



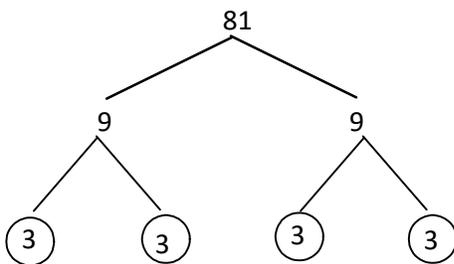
36 is a perfect square because it is a product of even pairs of numbers: 3 and 2, and 3 and 2.

$$\begin{aligned} \sqrt{36} &= \sqrt{2 \times 2 \times 3 \times 3} \\ \sqrt{36} &= \sqrt{(2 \times 2) \times (3 \times 3)} \\ \sqrt{36} &= 2 \times 3 \\ \sqrt{36} &= 6 \end{aligned}$$

Two identical pairs of numbers under a square root: one of each comes out. Nothing is left.

Check on Calculator!
 $\sqrt{36} = 6$

$\sqrt{81} = ?$

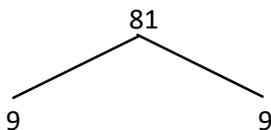


81 is a perfect square because it is a product of even pairs of numbers: 3 and 3, and 3 and 3.

$$\begin{aligned} \sqrt{81} &= \sqrt{3 \times 3 \times 3 \times 3} \\ \sqrt{81} &= \sqrt{(3 \times 3) \times (3 \times 3)} \\ \sqrt{81} &= 3 \times 3 \\ \sqrt{81} &= 9 \end{aligned}$$

Two identical pairs of numbers under a square root: one of each comes out. Nothing is left.

OR



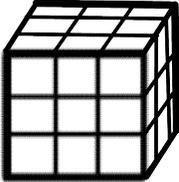
$$\begin{aligned} \sqrt{81} &= \sqrt{9 \times 9} \\ &= 9 \end{aligned}$$

Check on Calculator!
 $\sqrt{81} = 9$

Notice: when solving square roots using prime factorization either circle a pair of two identical numbers or multiple pairs of identical numbers.

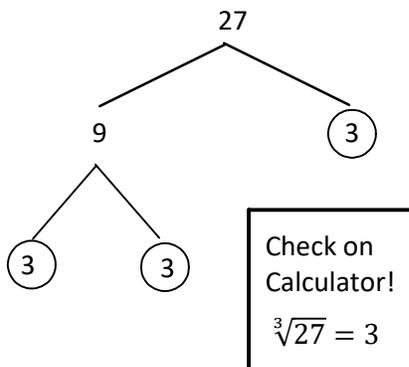
M8 - 3.2 - Solving Cube Roots Prime Factorization Notes

Perfect Cube: a number that is a product of the same three factors. $8 = 2 \times 2 \times 2 = 2^3$



$$\sqrt[3]{27} = 3 \quad 3 \times 3 \times 3 = 3^3 = 27$$

$\sqrt[3]{27} = ?$



Check on Calculator!
 $\sqrt[3]{27} = 3$

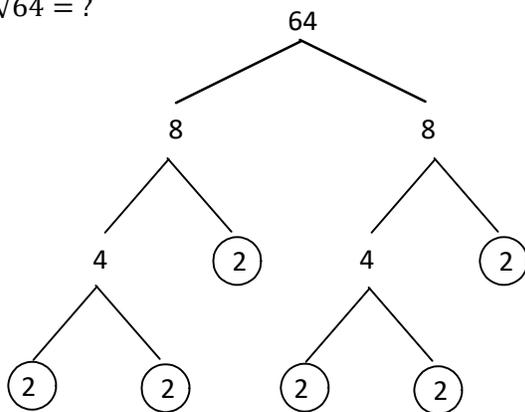
27 is a perfect cube because it is the product of three identical factors:

$$\begin{aligned} \sqrt[3]{27} &= \sqrt[3]{3 \times 3 \times 3} \\ \sqrt[3]{27} &= \sqrt[3]{\textcircled{3} \times \textcircled{3} \times \textcircled{3}} \\ &= \textcircled{3} \end{aligned}$$

Three identical numbers under a cube root: one comes out. Nothing is left.

OR Think about three identical numbers that multiply together to make that number

$\sqrt[3]{64} = ?$

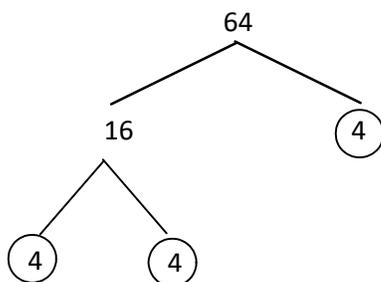


$$\begin{aligned} \sqrt[3]{64} &= \sqrt[3]{2 \times 2 \times 2 \times 2 \times 2 \times 2} \\ \sqrt[3]{64} &= \sqrt[3]{\textcircled{2} \times \textcircled{2} \times \textcircled{2} \times \textcircled{2} \times \textcircled{2} \times \textcircled{2}} \\ &= 2 \times 2 \\ &= \textcircled{4} \end{aligned}$$

Three identical numbers under a square root: one of each comes out. Nothing is left.

Check on Calculator!
 $\sqrt[3]{64} = 4$

OR



$$\begin{aligned} \sqrt[3]{64} &= \sqrt[3]{\textcircled{4} \times \textcircled{4} \times \textcircled{4}} \\ &= \textcircled{4} \end{aligned}$$

Notice: when solving cube roots using prime factorization either circle a triplet of three identical numbers or multiple triplets of identical numbers.