

C12 - 5.0 - Fundamental Theorem Part II/AP Notes

$$\frac{d}{dx} \int_0^x x^2 dx = x^2 \times 1 - 0^2 \times 0 \\ = x^2$$

Taking a Derivative of an Integral Cancels each other out*

Substitute the Upper Limit

$$\frac{d}{dx} \int_0^{x^2} (x+2) dx = (x^2 + 2) \times 2x - (0 - 2) \times 0 \\ = 2x(x^2 + 2)$$

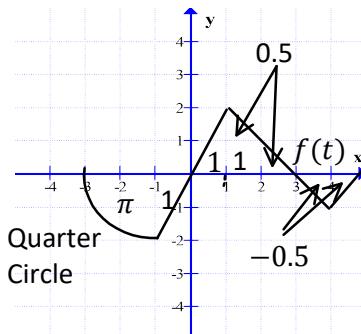
Multiply by the Derivative of the Upper Limit

Substitute the Lower Limit

Multiply by the Derivative of the Lower Limit

$$\frac{d}{dx} \int_1^{x^2} \frac{\sin t}{t} dt = \frac{\sin x^2}{x^2} \times 2x - \frac{\sin 1}{1} \times 0 \\ = \frac{2\sin x^2}{x}$$

$$\int_1^b \frac{1}{x^2} dx = -\frac{1}{x} \Big|_1^b \\ = -\frac{1}{b} - \left(-\frac{1}{1}\right) \\ = \frac{1}{b} + 1$$



$$g(x) = \int_1^x f(t) dt$$

$$g(3) = \int_1^3 f(t) dt = 1 + 0.5 + 0.5 = 2$$

$$g(-3) = \int_1^{-3} f(t) dt = - \int_{-3}^1 f(t) dt = -(-\pi - 1 + 1) = \pi$$

$$g'(3) = \frac{d}{dx} \int_1^3 f(t) dt \\ = f(3) = 0$$

$$g''(3) = \frac{d}{dx} \frac{d}{dt} \int_1^3 f(t) dt \\ = f'(x) = -1$$

$$g(x) = \int f(t) dt \\ g'(x) = f(t) \\ g''(x) = f'(t)$$

$$g(x) CP \quad g'(x) = 0 \quad \longrightarrow \quad f(x) = 0$$

$$\& g'(x) > 0 \rightarrow g'(x) < 0 \quad x = 3 \quad \& f(x) > 0 \rightarrow f(x) < 0$$

$$\boxed{OR} \quad \& g'(x) < 0 \rightarrow g'(x) > 0 \quad x = 0 \quad \& f(x) < 0 \rightarrow f(x) > 0$$

Loc Min

| t | $g(x)$ | $g'(x)$ | $g''(x)$ |
|-----|--------|---------|----------|
| -3 | π | 0 | und |
| -1 | 0 | -2 | und |
| 0 | -1 | 0 | 2 |
| 1 | 0 | 2 | und |
| 2 | 1.5 | 1.5 | -1 |
| 3 | 2 | 0 | -1 |
| 4 | 1.5 | -1 | und |
| 5 | 1 | 0 | 1 |

$$g(x) IP \quad g''(x) = 0 \quad \longrightarrow \quad f'(x) = 0$$

$$\& g''(x) > 0 \rightarrow g''(x) < 0 \quad x = 1 \quad \& f'(x) > 0 \rightarrow f'(x) < 0$$

$$\boxed{OR} \quad \& g''(x) < 0 \rightarrow g''(x) > 0 \quad x = -1, 4 \quad \& f'(x) < 0 \rightarrow f'(x) > 0$$

Check Endpoints

$g(x)$ Abs Max

$(-3, \pi)$