

C12 - 1.7 - Limit Slope Notes

Find average slope over domain, equation of the secant line, and sketch only [1,2].

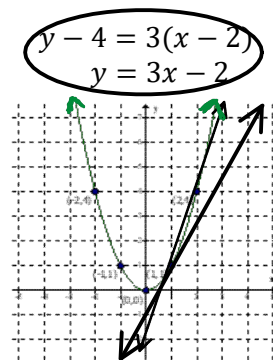
$$f(x) = x^2 ; [1,2], [1,1.1], [1,1.01].$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{1.21 - 1}{1.1 - 1} = 2.1$$

$$m = \frac{1.0201 - 1}{1.01 - 1} = 2.01$$

$$m = \frac{1.002001 - 1}{1.001 - 1} = 2.001$$



Find the instantaneous slope, equation of the tangent line, and sketch.

$$f(x) = x^2 ; x = 1$$

$$f(1) = 1 \quad (1,1)$$

$$y - 1 = 2(x - 1)$$

$$y = 2x - 1$$

Method 1*

$$m = f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

$$m = f'(1) = \lim_{x \rightarrow 1} \frac{x^2 - f(1)}{x - 1}$$

$$= \lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$$

$$= \lim_{x \rightarrow 1} \frac{(x + 1)(x - 1)}{(x - 1)}$$

$$= \lim_{x \rightarrow 1} (x + 1)$$

$$= 1 + 1$$

$$m = f'(1) = 2$$

Method 2*

$$m = f'(a) = \lim_{h \rightarrow 0} \frac{f(a + h) - f(a)}{h}$$

$$m = f'(1) = \lim_{h \rightarrow 0} \frac{f(1 + h) - f(1)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{(1 + h)^2 - (1)^2}{h}$$

$$= \lim_{h \rightarrow 0} \frac{1 + 2h + h^2 - 1}{h}$$

$$= \lim_{h \rightarrow 0} \frac{2h + h^2}{h}$$

$$= \lim_{h \rightarrow 0} \frac{h(2 + h)}{h}$$

$$= \lim_{h \rightarrow 0} (2 + h)$$

$$= 2 + 0$$

$$m = f'(1) = 2$$

Find average slope over domain, equation of the secant line, and sketch only [1,2].

$$f(x) = x^3 ; [1,2], [1,1.1], [1,1.01].$$

Find the instantaneous slope, equation of the tangent line, and sketch.

$$f(x) = x^2 - 2x ; x = 3$$

$$f(x) = x^3 ; x = -1$$

$$f(x) = x^4 ; x = 1$$

$$f(x) = \frac{1}{x+2} ; x = 2$$

$$f(x) = \sqrt{x+1} ; x = 0$$

$$f(x) = \frac{1}{\sqrt{x+3}} ; x = 1$$